

EVALUATION
ONLINE LEARNING
LINKS WITH OPTIMIZATION AND GAMES
UNIVERSITÉ PARIS–SACLAY



HYPERBOLIC ENTROPY

Let $d \geq 1$. The paper¹ [GHS20] studies an algorithm based on the hyperbolic entropy:

$$H_\beta(x) = \sum_{i=1}^d \left(x_i \operatorname{arcsinh} \left(\frac{x_i}{\beta} \right) - \sqrt{x_i^2 + \beta^2} \right), \quad x \in \mathbb{R}^d.$$

- 1) Rewrite the algorithm and the proofs of the regret bounds using the notation and tools from the course.
- 2) Generalize the algorithm and regret bounds from the paper using the theory from the course.

REFERENCES

[GHS20] Udaya Ghai, Elad Hazan, and Yoram Singer. Exponentiated gradient meets gradient descent. In *Algorithmic learning theory*, pages 386–407. PMLR, 2020.

¹the paper is available at <https://proceedings.mlr.press/v117/ghai20a/ghai20a.pdf>

